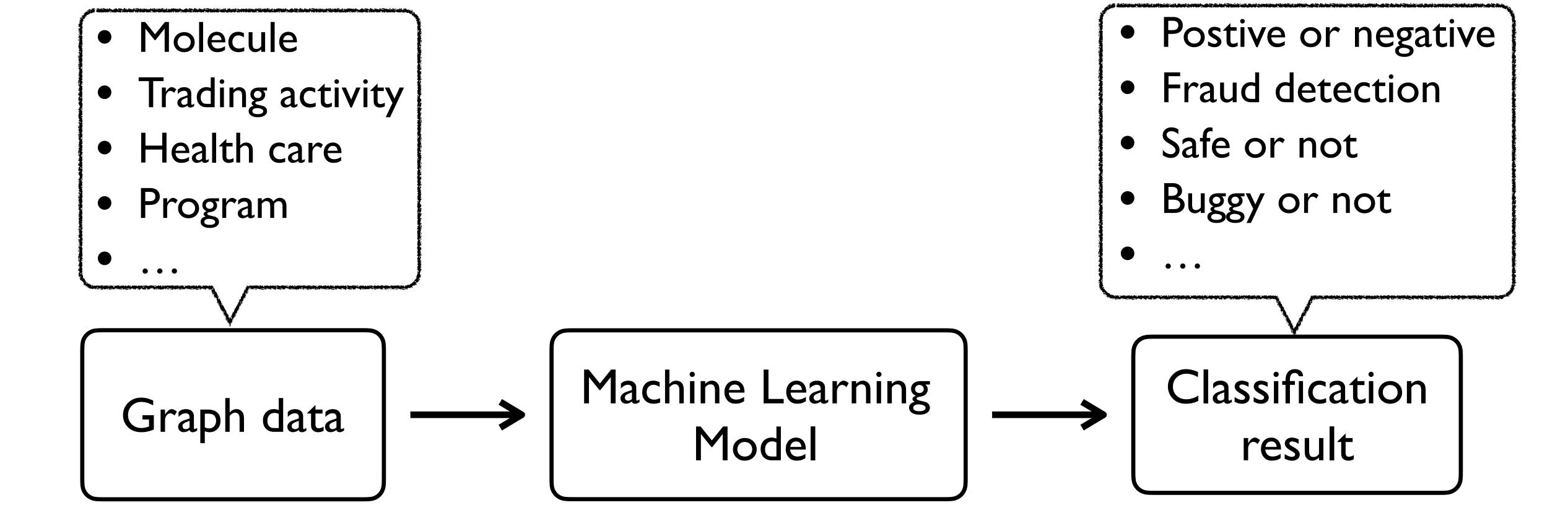
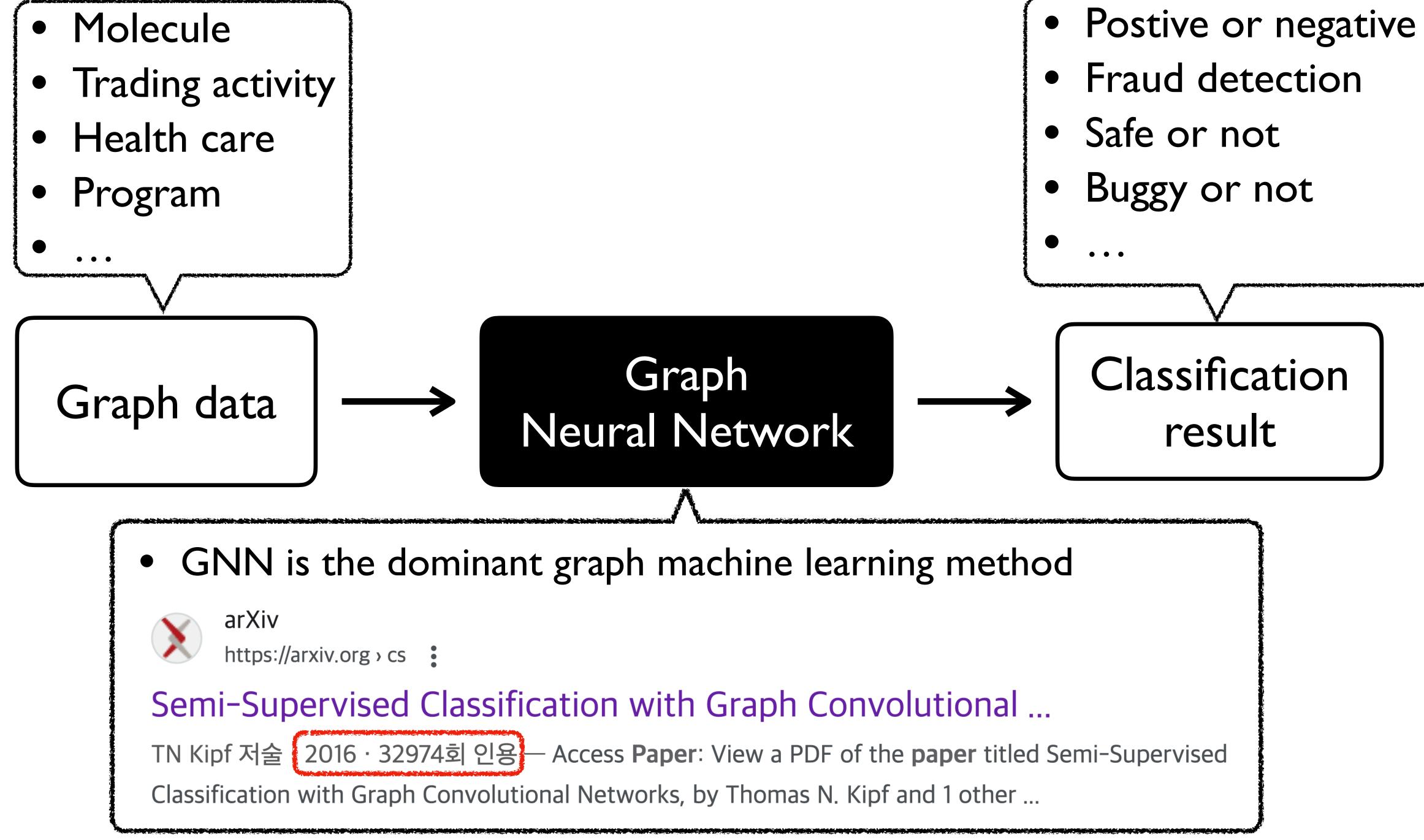


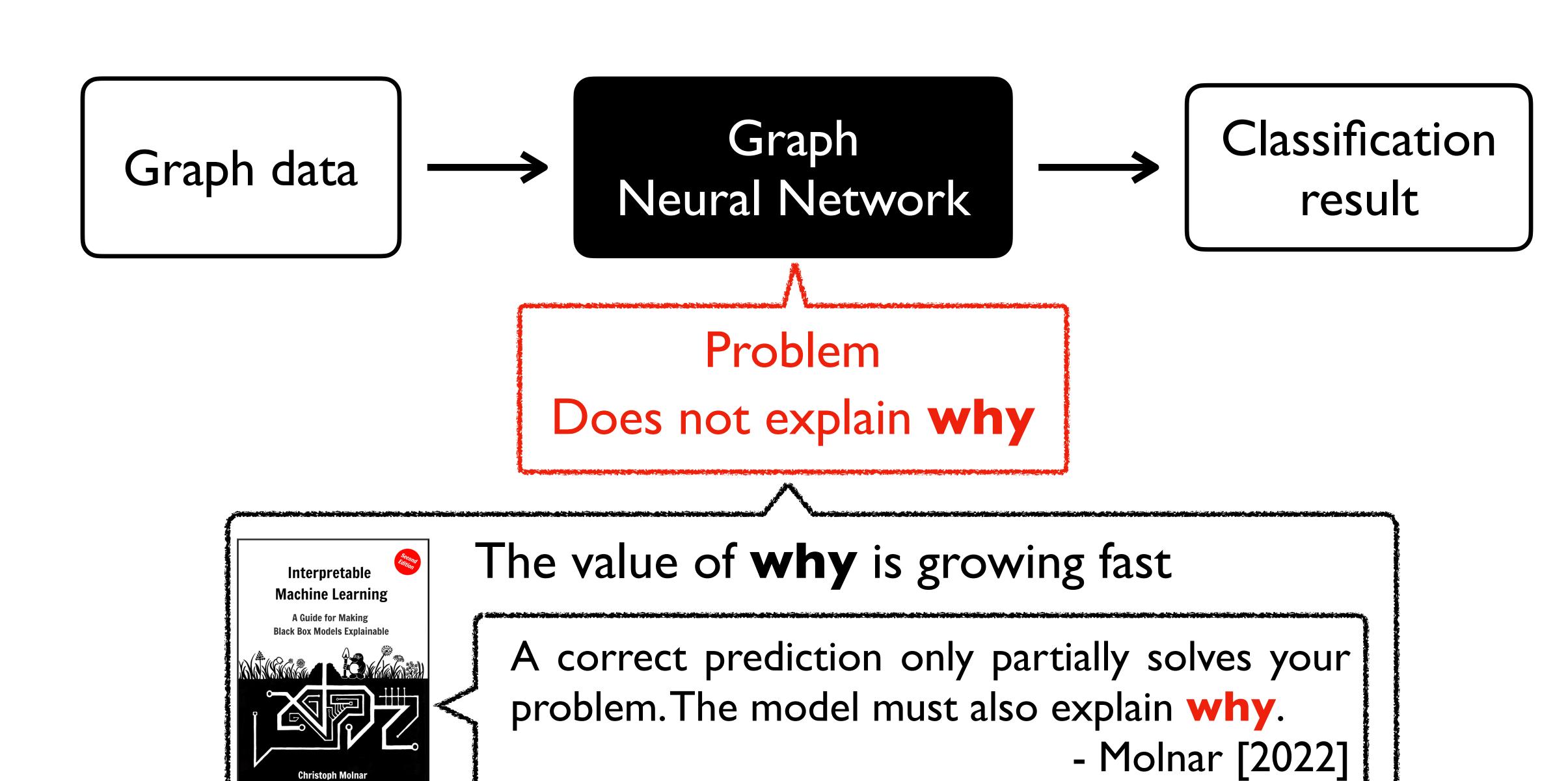
PL4XGL: A Programming Language Approach to Explainable Graph Learning

Minseok Jeon

18 September 2025 @ IC637









Graph Neural Network

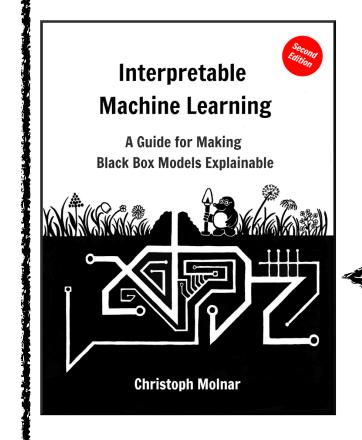
Classification result

- Health care
- Trading activity
- •

Problem

Does not explain why

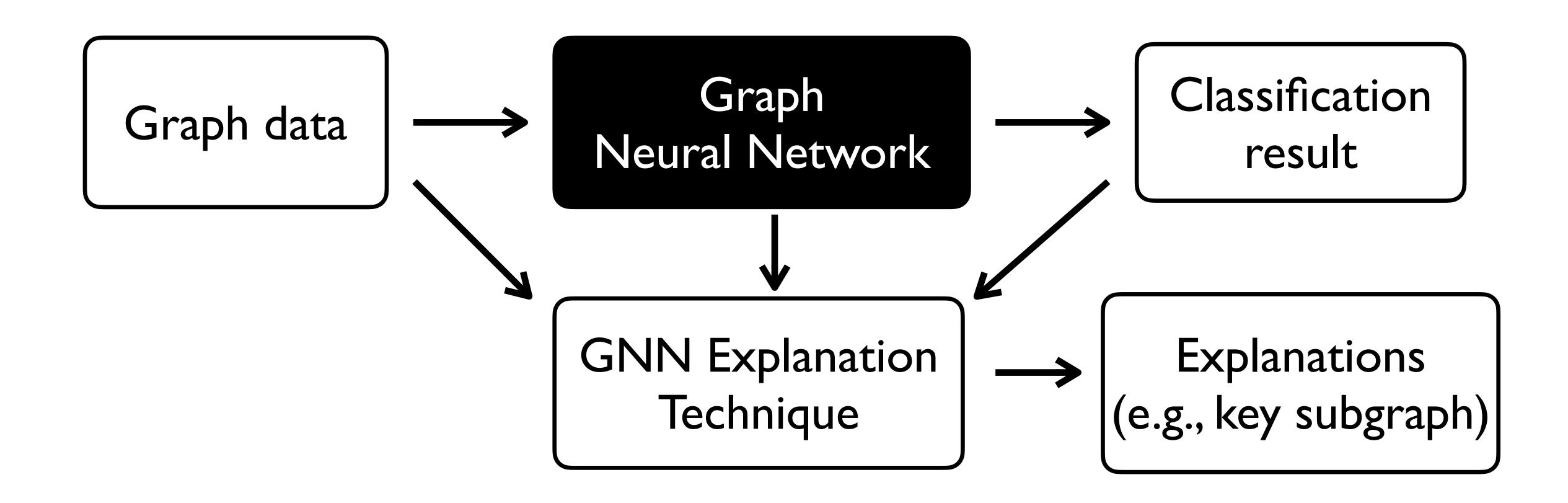
- Safe or not
- Fraud or not
- •

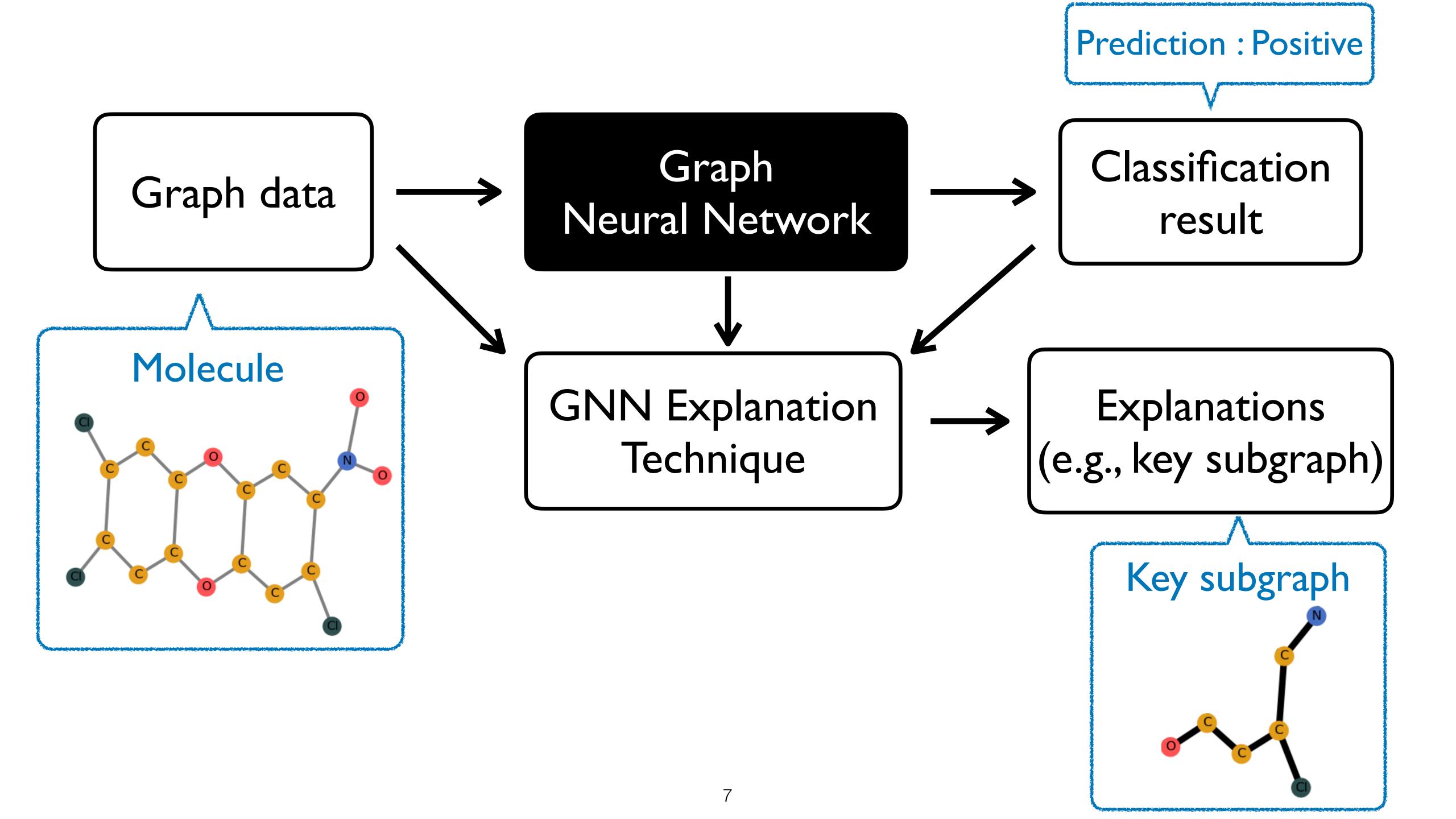


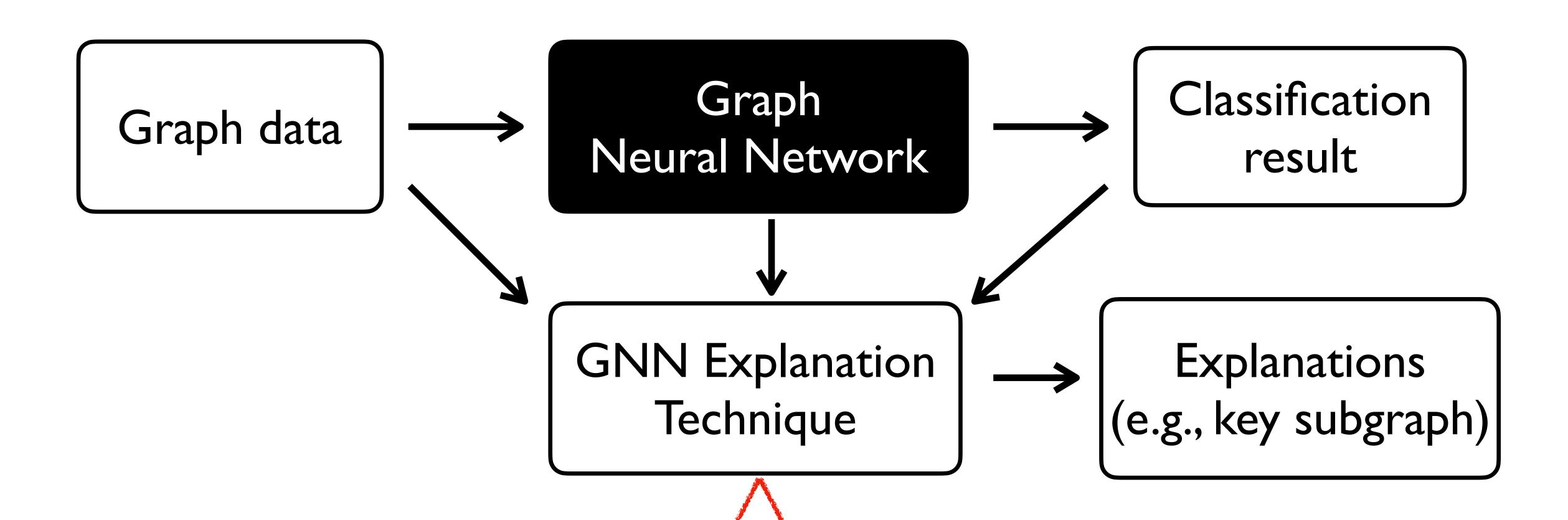
The value of why is growing fast

A correct prediction only partially solves your problem. The model must also explain why.

- Molnar [2022]







Two key limitations

- Additional (expensive) explanation cost is required
- The explanations are not guaranteed to be correct

• PL4XGL: inherently explainable graph machine learning method

Graph data —

PL4XGL

Classification result & correct explanation

Graph Description Language (GDL)

```
Programs P ::= \overline{\delta} \text{ target } t \in \mathbb{P} = \mathbb{D}^* \times \mathbb{T}
Descriptions \delta ::= \delta_V \mid \delta_E \in \mathbb{D} = \mathbb{D}_V \uplus \mathbb{D}_E

Node Descriptions \delta_V ::= \text{node } x < \overline{\phi} > ? \in \mathbb{D}_V = \mathbb{X} \times \Phi^d

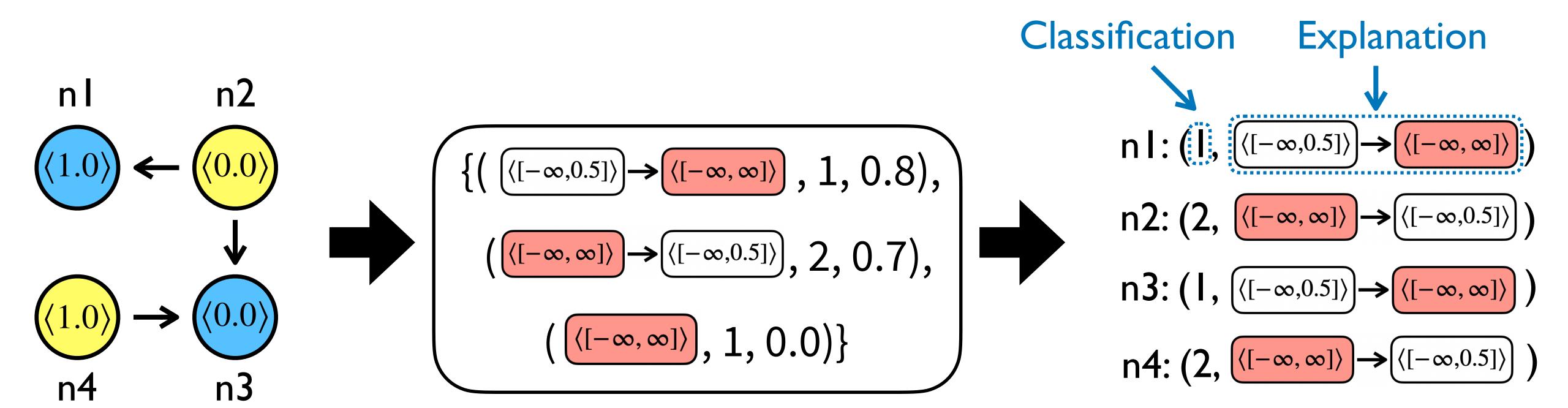
Edge Descriptions \delta_E ::= \text{edge } (x,x) < \overline{\phi} > ? \in \mathbb{D}_E = \mathbb{X} \times \mathbb{X} \times \Phi^c

Target Symbols t ::= \text{node } x \mid \text{edge } (x,x) \mid \text{graph} \in \mathbb{T} = \mathbb{X} \uplus (\mathbb{X} \times \mathbb{X}) \uplus \{\epsilon\}

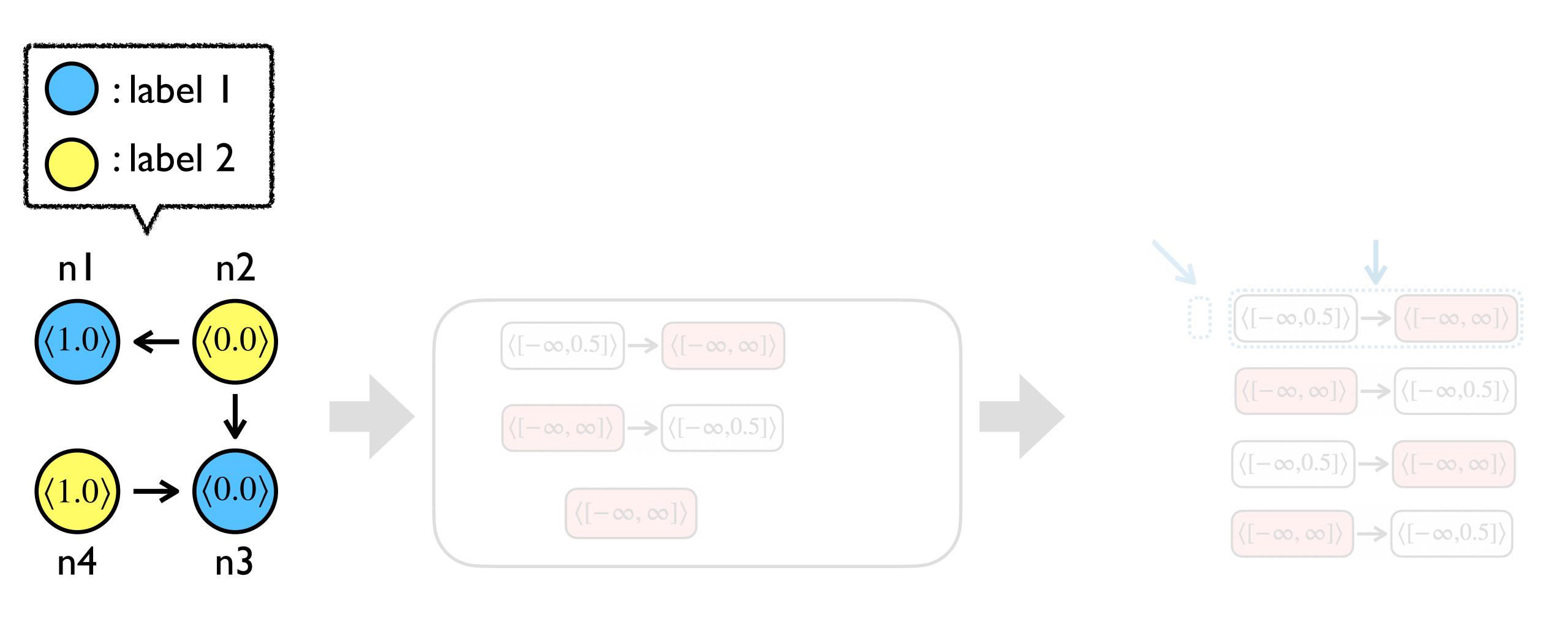
Intervals \phi ::= [n^?, n^?] \in \Phi = (\mathbb{R} \uplus \{-\infty\}) \times (\mathbb{R} \uplus \{\infty\})

Real Numbers n ::= 0.2 \mid 0.7 \mid 6 \mid -8 \dots \in \mathbb{R}

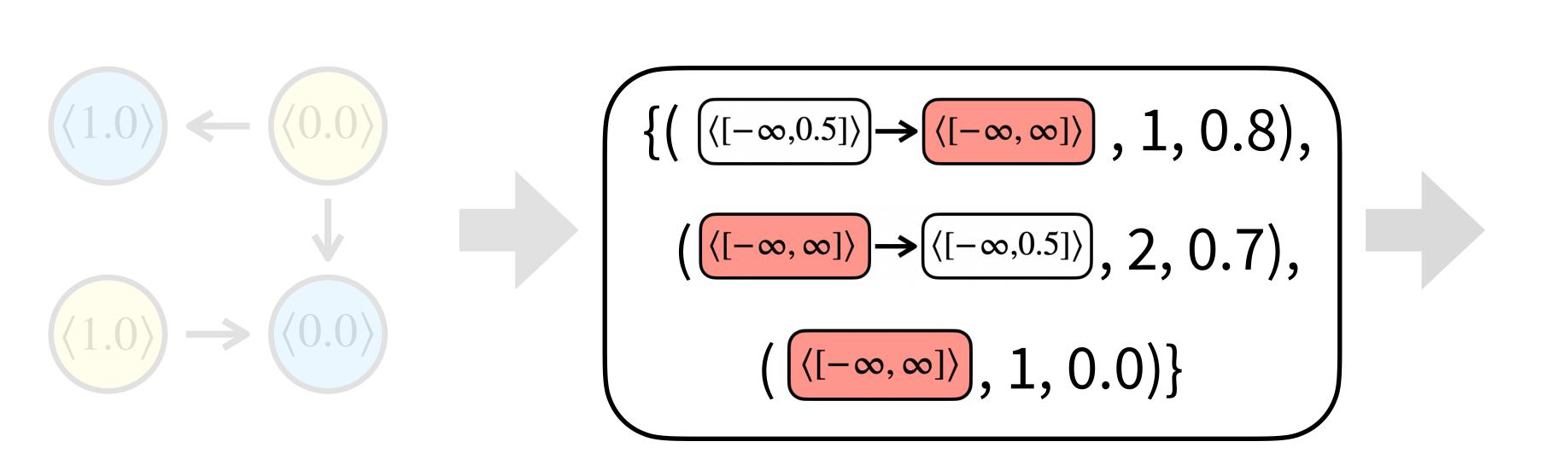
Variables x ::= x \mid y \mid z \mid \dots \in \mathbb{X}
```

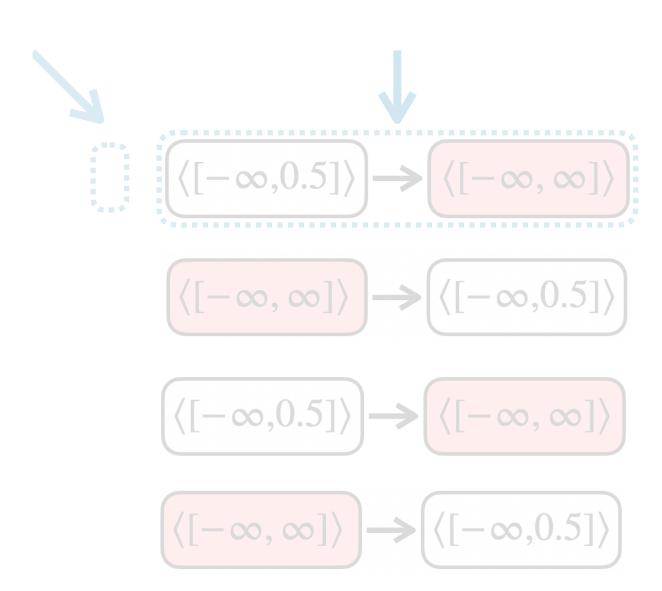


Our model

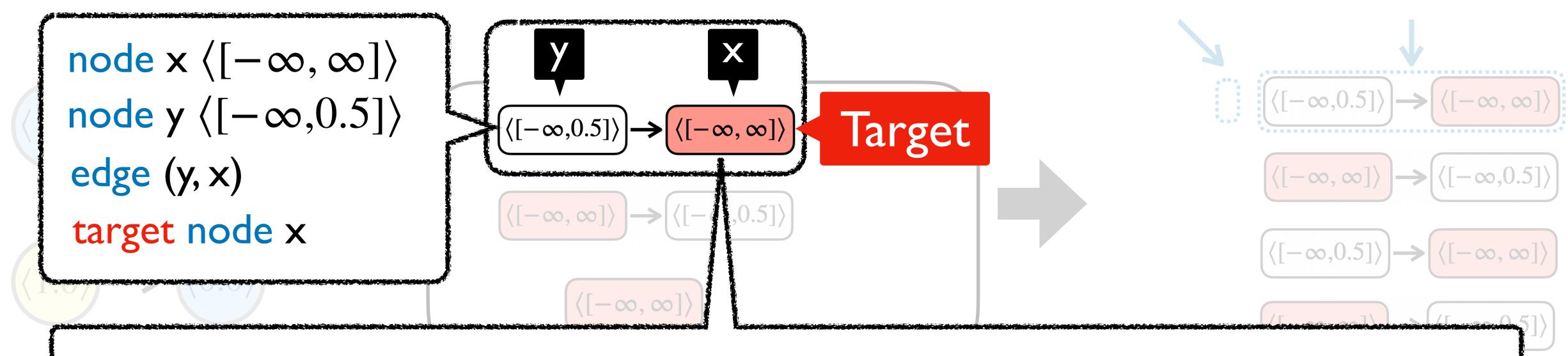


Graph data

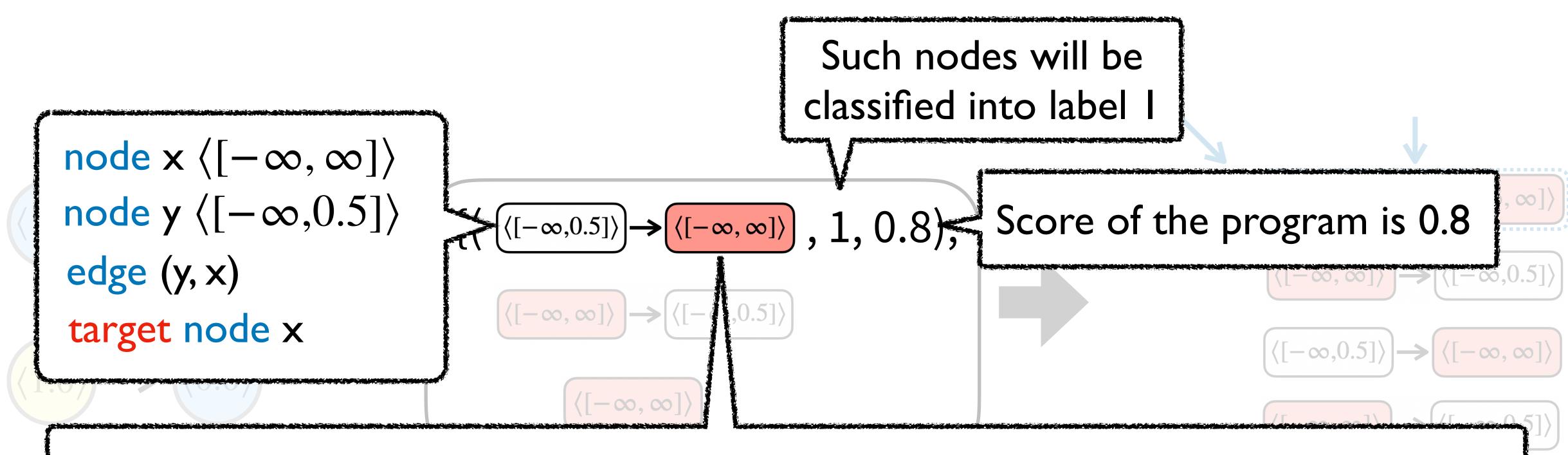




Our model

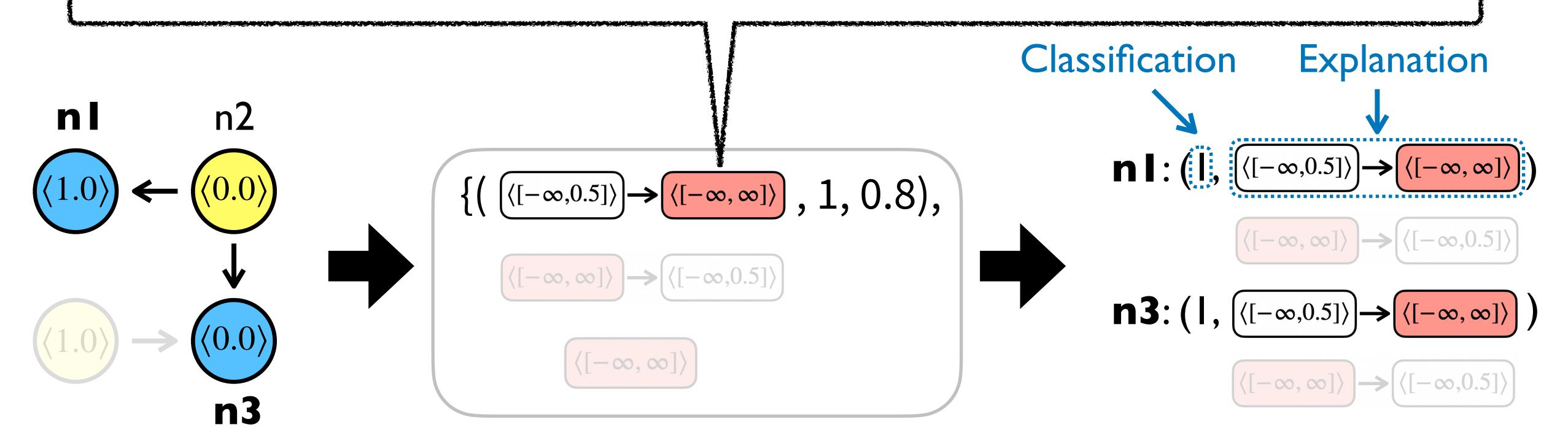


"Nodes having a predecessor whose feature value is equal or less than 0.5"



"Nodes having a predecessor whose feature value is equal or less than 0.5"

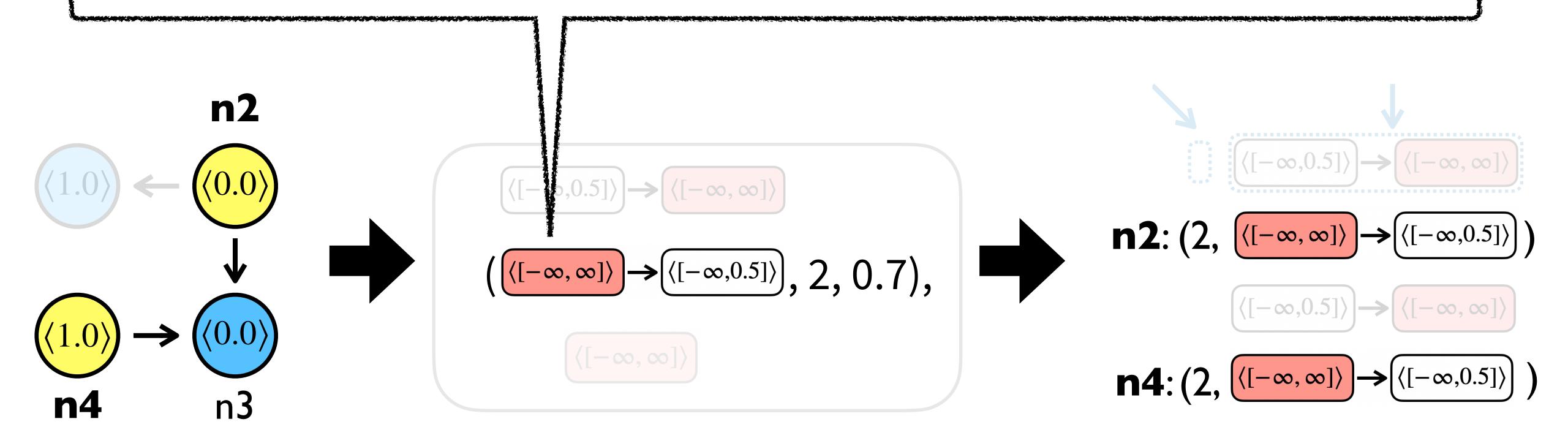
"Nodes having a predecessor whose feature value is equal or less than 0.5"



Graph data

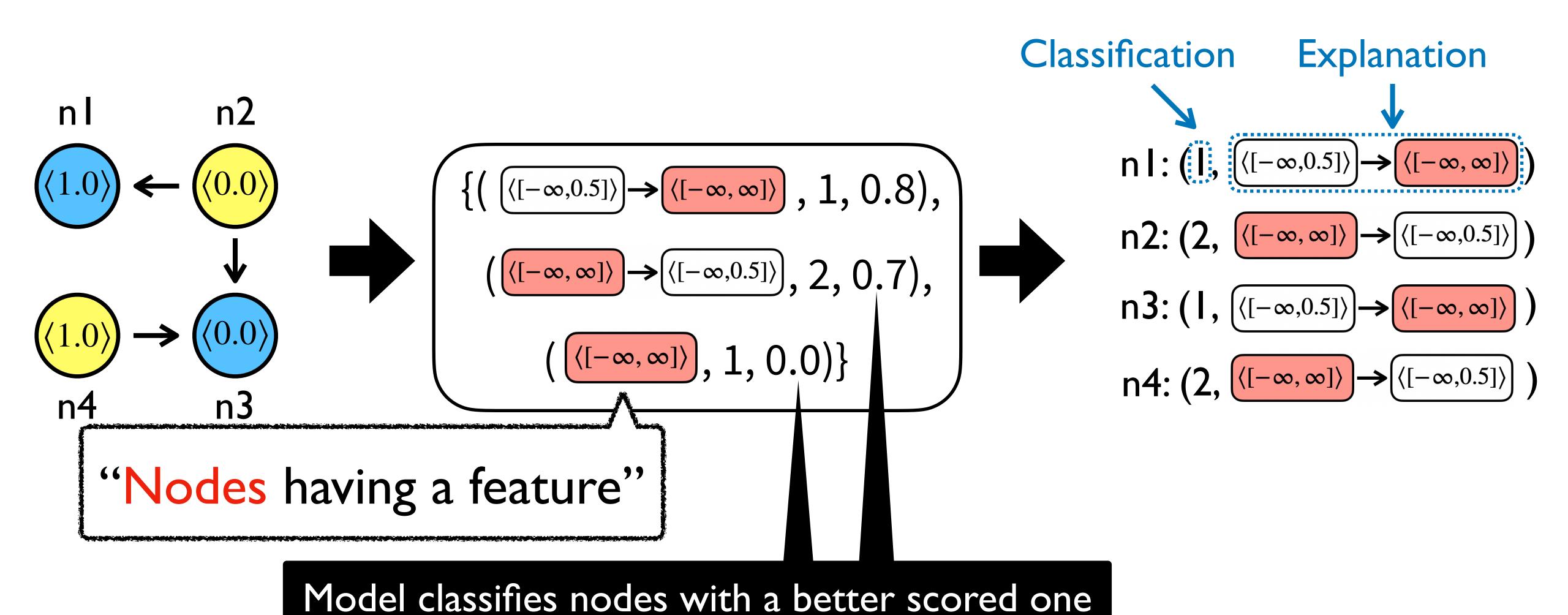
Our model

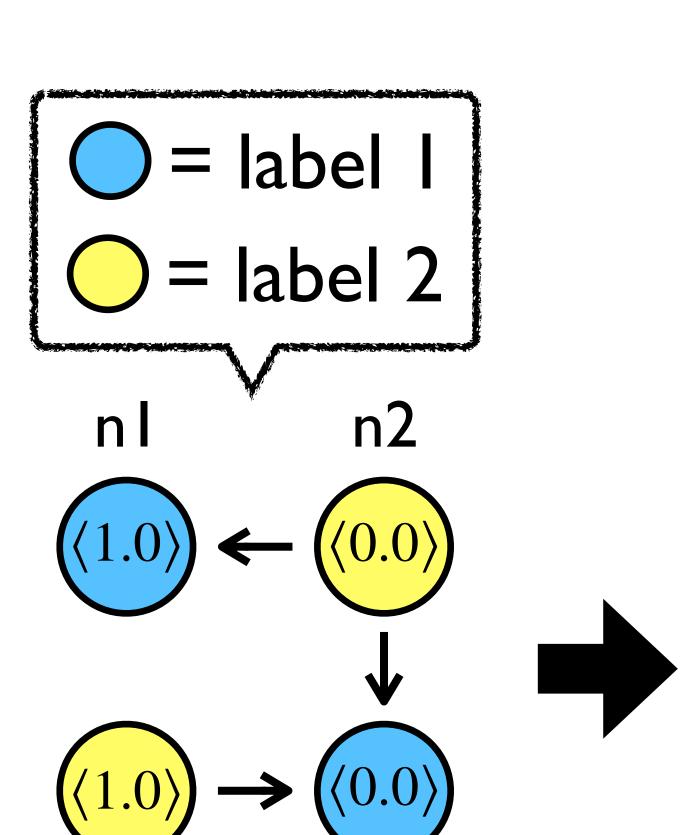
"Nodes having a successor whose feature value is equal or less than 0.5"



Graph data

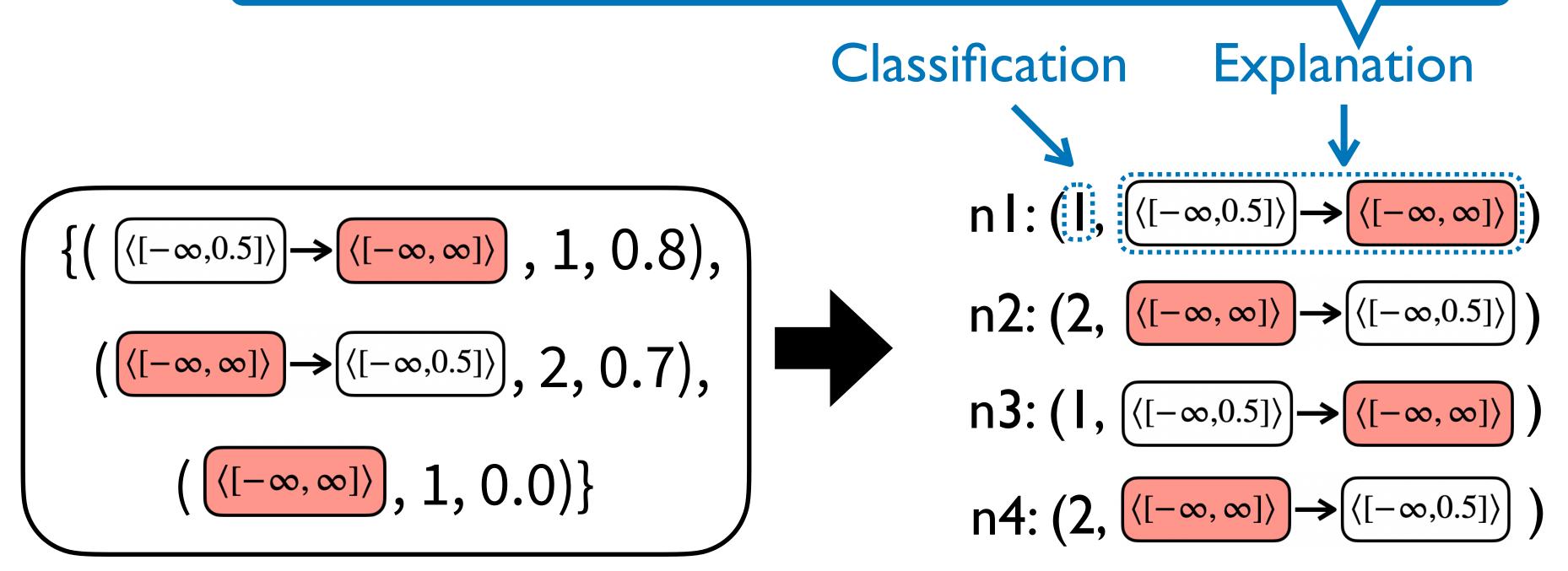
Our model





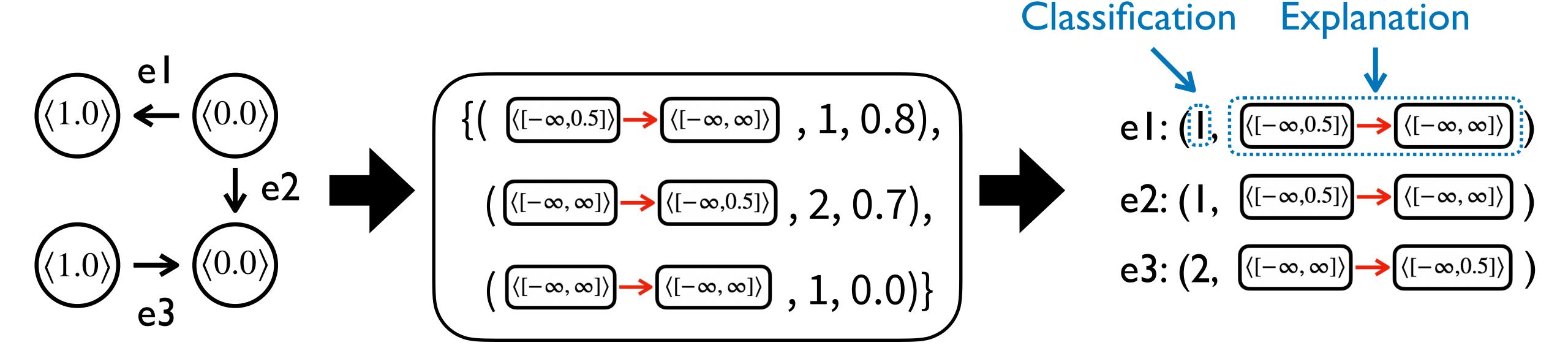
n3

- No additional explanation cost
- Explanations are guaranteed to be correct



Graph data

Our model



Our model (edge classification)

```
\mathsf{node} \times \langle [-\infty, 0.5] \rangle
node y \langle [-\infty, \infty] \rangle
edge (x, y)
target edge (x, y)
     ([-\infty,0.5]) \rightarrow (([-\infty,\infty]), 1, 0.8),
      ([-\infty,\infty]) \rightarrow (([-\infty,0.5]), 2, 0.7),
     (([-\infty,\infty])) \rightarrow (([-\infty,\infty])), 1, 0.0)
   \mathsf{node}\,\mathsf{x}\,\langle[-\infty,\infty]\rangle
   node y \langle [-\infty, \infty] \rangle
   edge (x, y)
target edge (x, y)
```

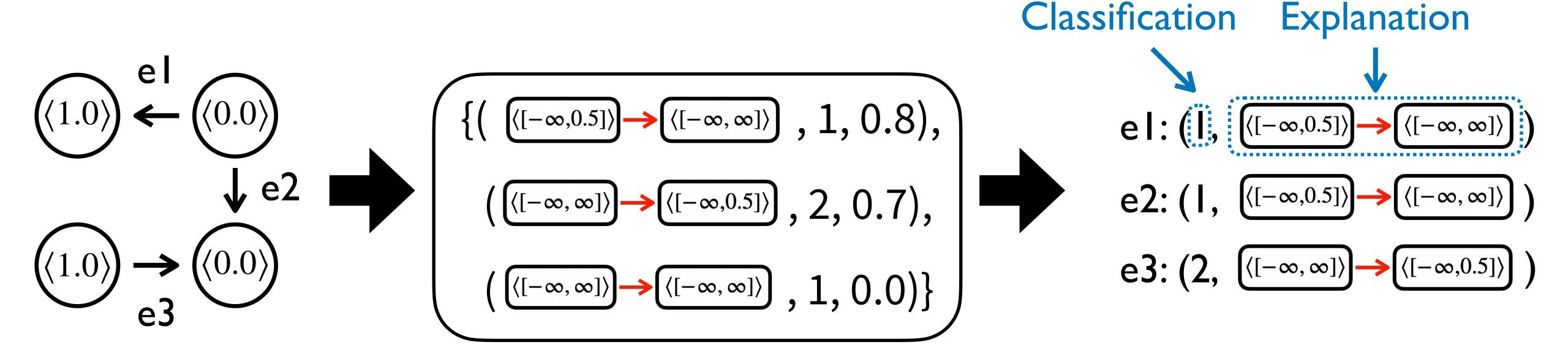
 $\langle [-\infty, \infty] \rangle \longrightarrow \langle [-\infty, 0.5] \rangle$

 $\mathsf{node}\,\mathsf{x}\,\langle[-\infty,\infty]\rangle$

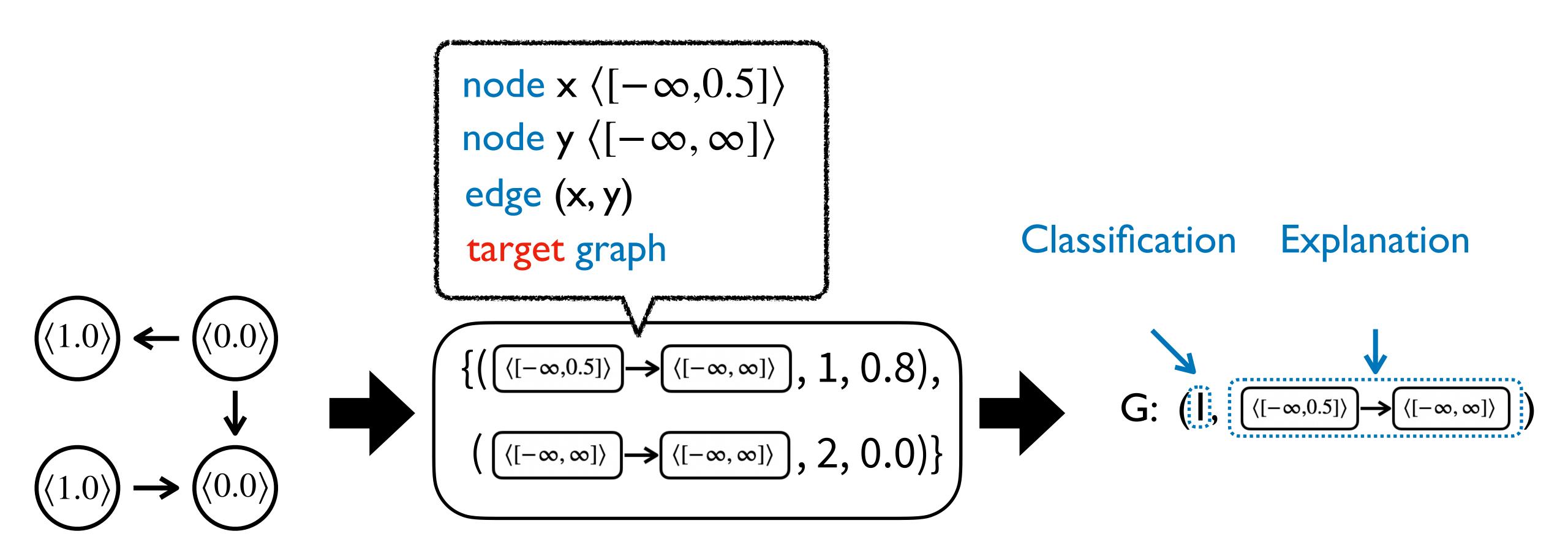
node y $\langle [-\infty, 0.5] \rangle$

target edge (x, y)

edge (x, y)

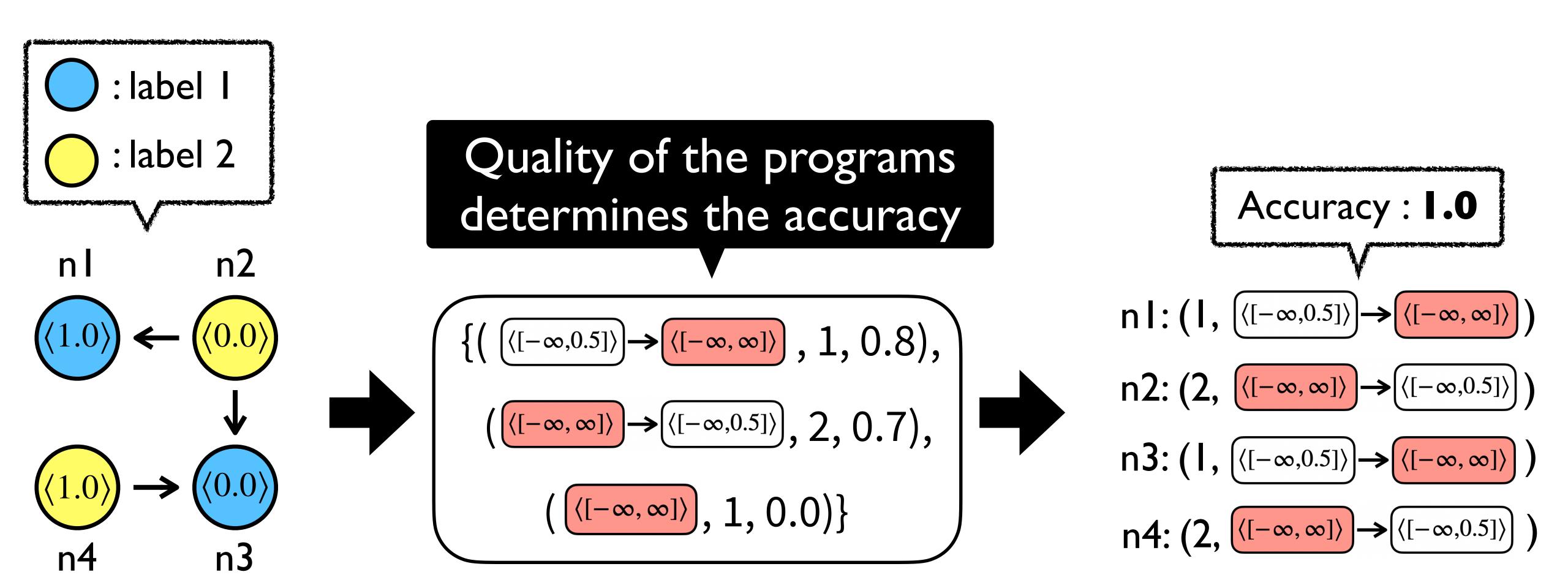


Our model (edge classification)

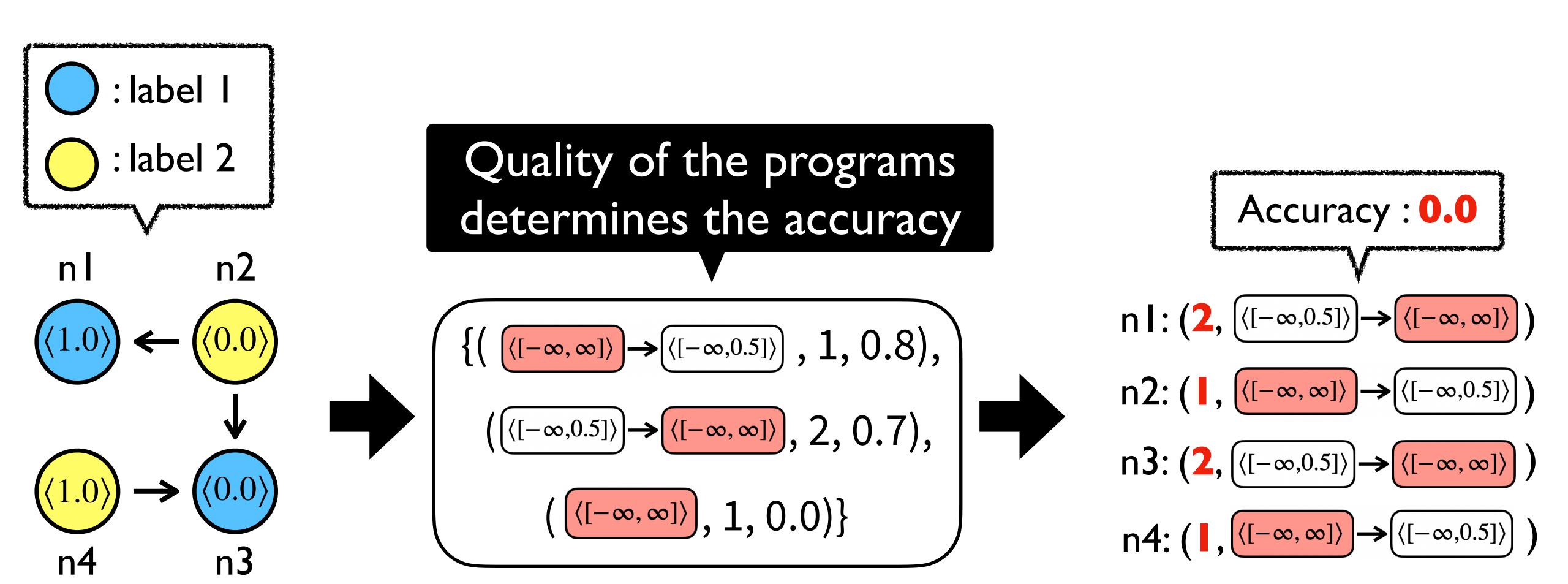


Graph G

Our model (graph classification)

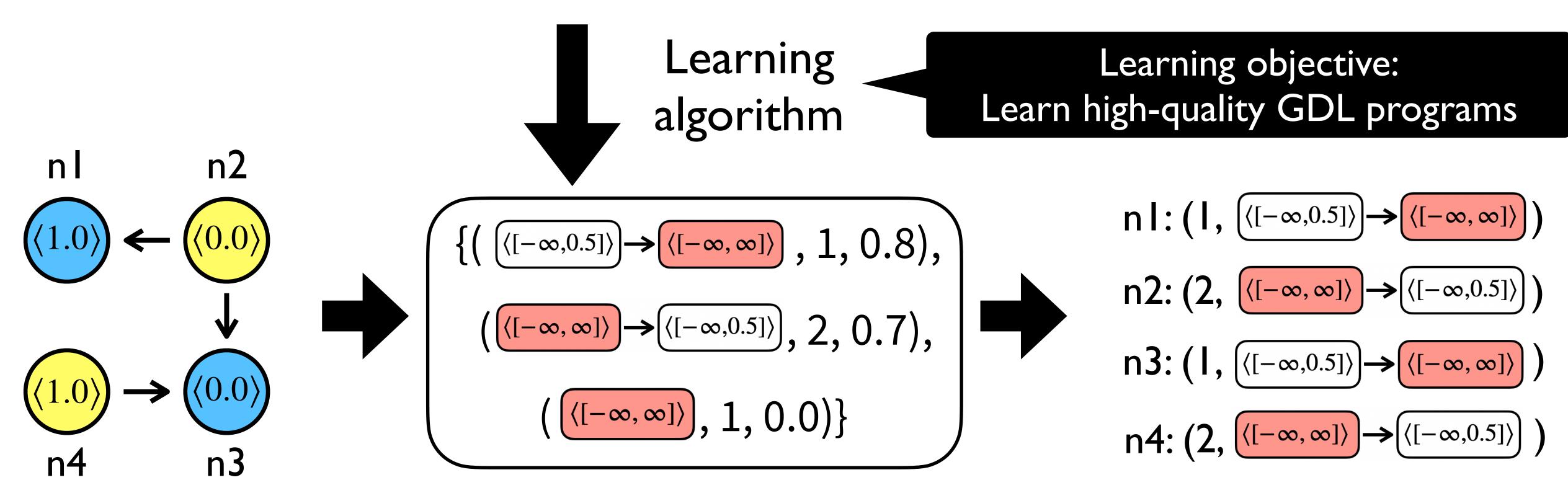


Our model (node classification)

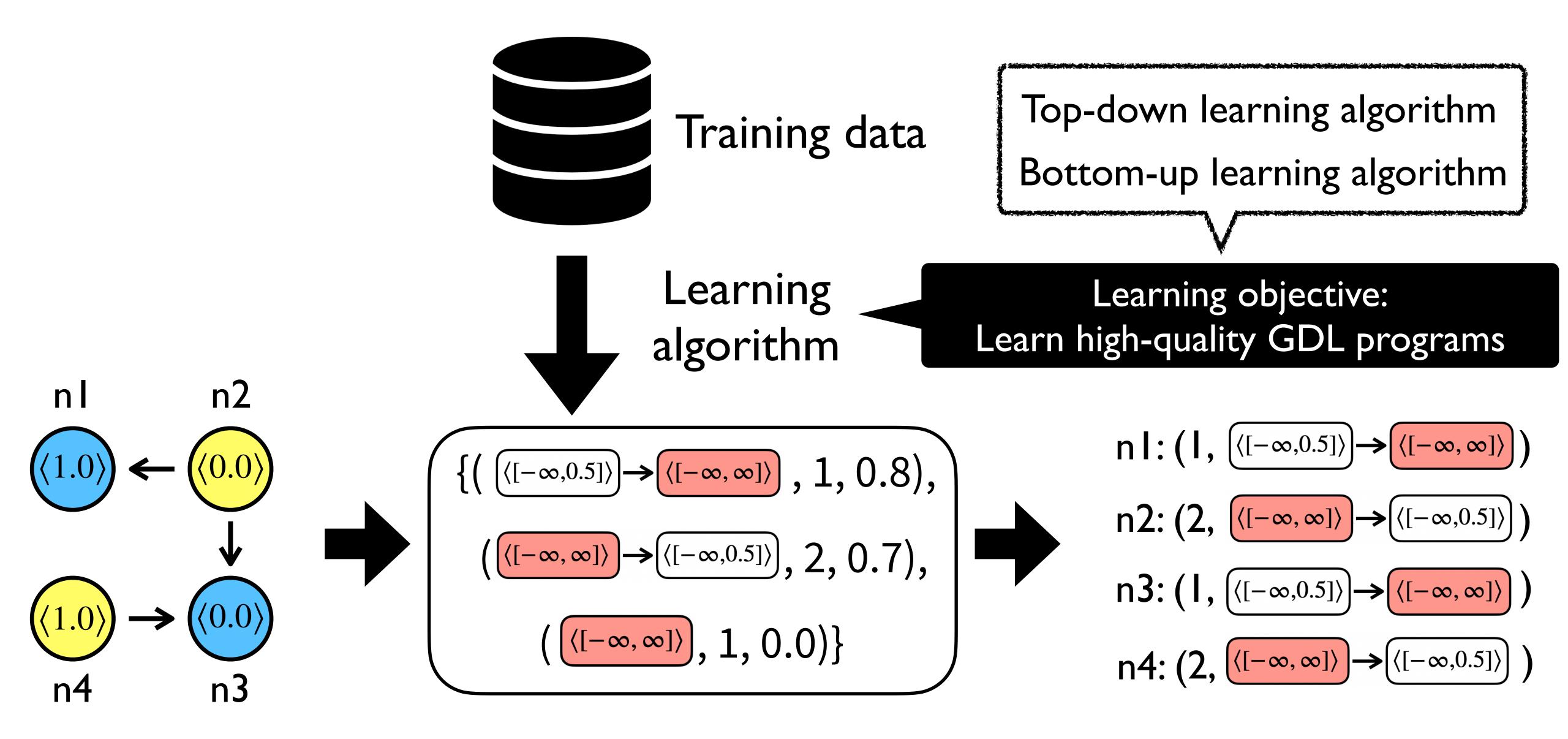


Our model (node classification)





Our model



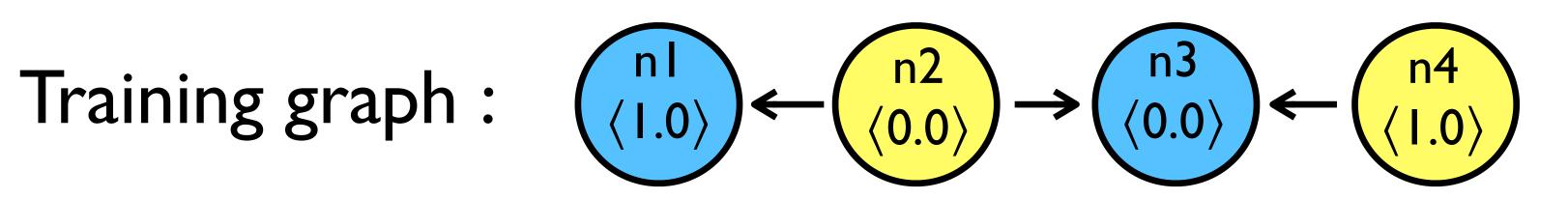
Our model

GDL Program Learning Algorithm

Learning Objective

Generate a GDL program that includes the target node n1 and precisely describes the nodes belong to the label 1 (O)

Top-down Learning Algorithm



Target node = n1

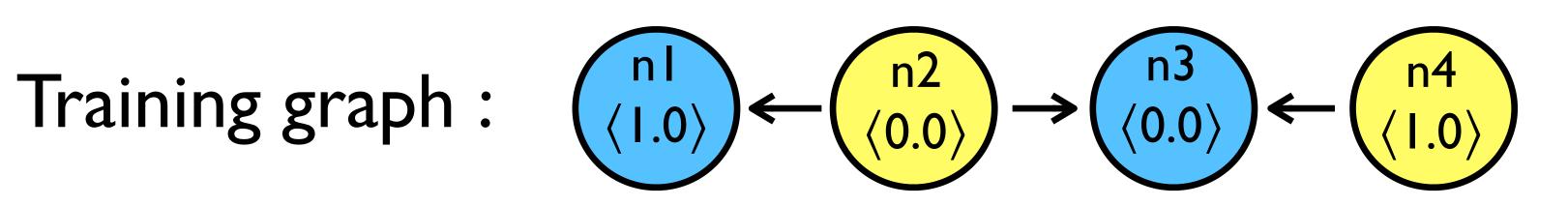
: label I

: label 2

(I) Starts from the most general program

```
\langle [-\infty, \infty] \rangle | Score: 0.4
```

Top-down Learning Algorithm



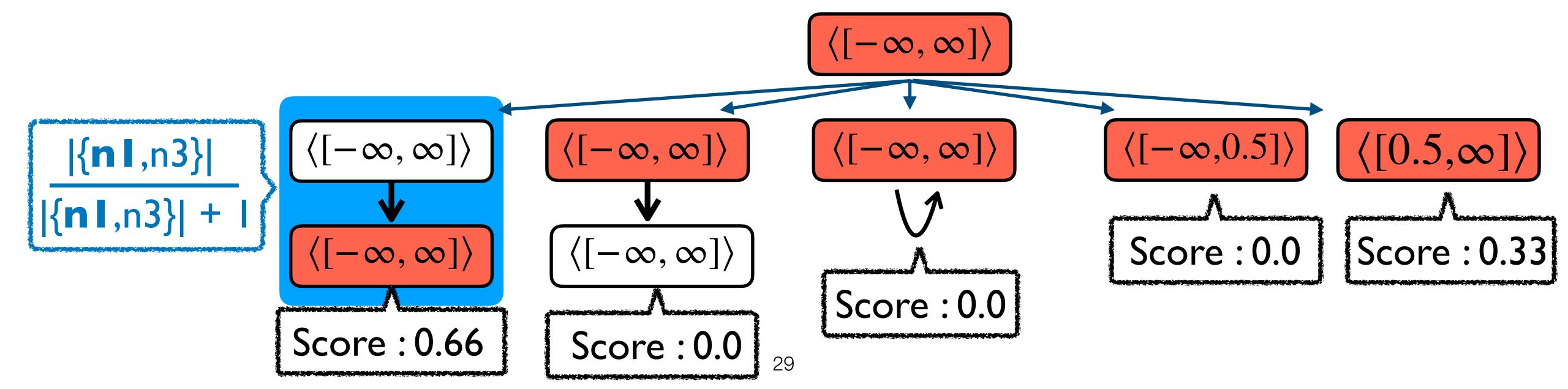
Target node = n1

: label I

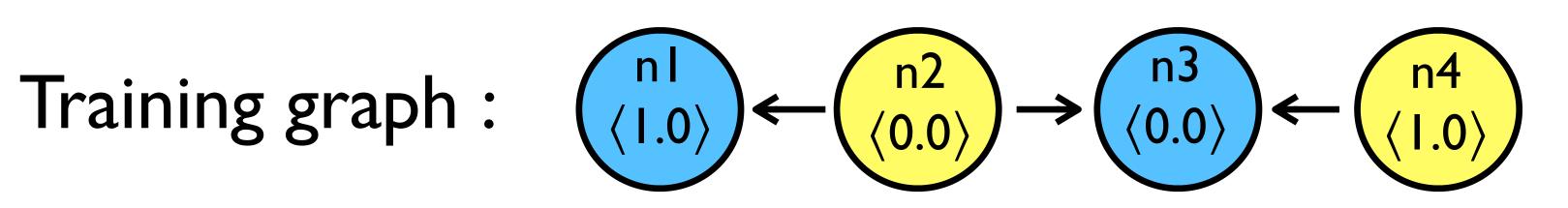
: label 2

- (I) Starts from the most general program $([-\infty, \infty])$ Score : 0.4

(2) Enumerate possible specified programs and choose a better scored one.



Top-down Learning Algorithm



Target node = n1

- : label I
- : label 2
- (I) Starts from the most general program $([-\infty, \infty])$ Score: 0.4

$$\langle [-\infty, \infty] \rangle$$
 Score: 0.4

(2) Enumerate possible specified programs and choose a better scored one.

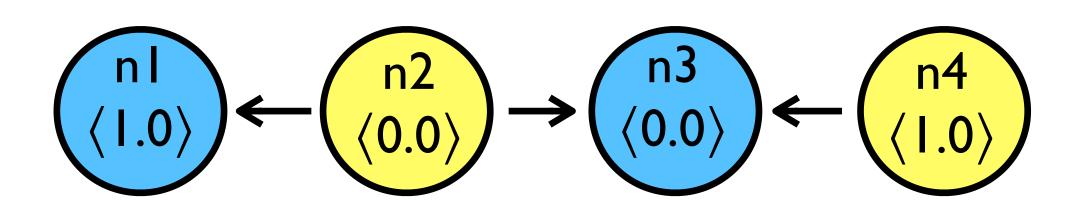
$$\langle [-\infty, \infty] \rangle \rightarrow \langle [-\infty, \infty] \rangle \langle [-\infty, \infty] \rangle$$
 Score: 0.66

- (3) Repeat (2) until no better program is enumerated
- (4) Return the current program

$$([-\infty,\infty]) \rightarrow ([-\infty,\infty])$$
, label 1, 0.66)

Bottom-up Learning Algorithm

Training graph:



Target node = n1

: label I

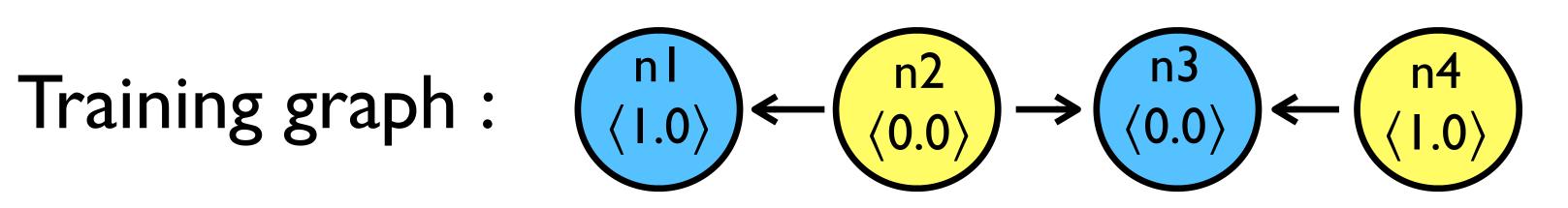
: label 2

(I) Starts from the most specific program

```
 \leftarrow \boxed{\langle [0.0, 0.0] \rangle} \leftarrow \boxed{\langle [0.0, 0.0] \rangle} \leftarrow \boxed{\langle [1.0, 1.0] \rangle} \leftarrow \boxed
```

```
node vI \( [1.0,1.0] \)
node v2 \( [0.0,0.0] \)
node v3 \( [0.0,0.0] \)
node v4 \( [0.0,0.0] \)
edge \( (v2, v1) \)
edge \( (v2, v3) \)
edge \( (v4, v3) \)
target node vI
```

Bottom-up Learning Algorithm



Target node = n1

: label I

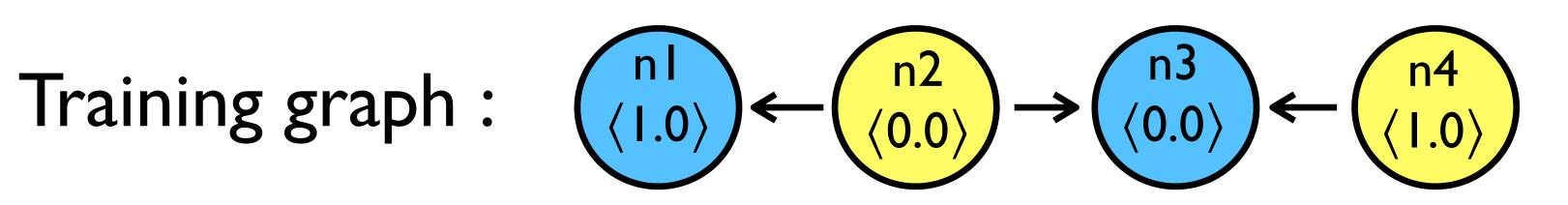
: label 2

(1) Starts from the most specific program

$$\langle [1.0, 1.0] \rangle \leftarrow \langle [0.0, 0.0] \rangle \leftarrow \langle [0.0, 0.0] \rangle \leftarrow \langle [1.0, 1.0] \rangle \leftarrow Score : 0.5$$

(2) Enumerate possible generalized programs and choose an equal or better scored one

Bottom-up Learning Algorithm



Target node = n1

: label I

: label 2

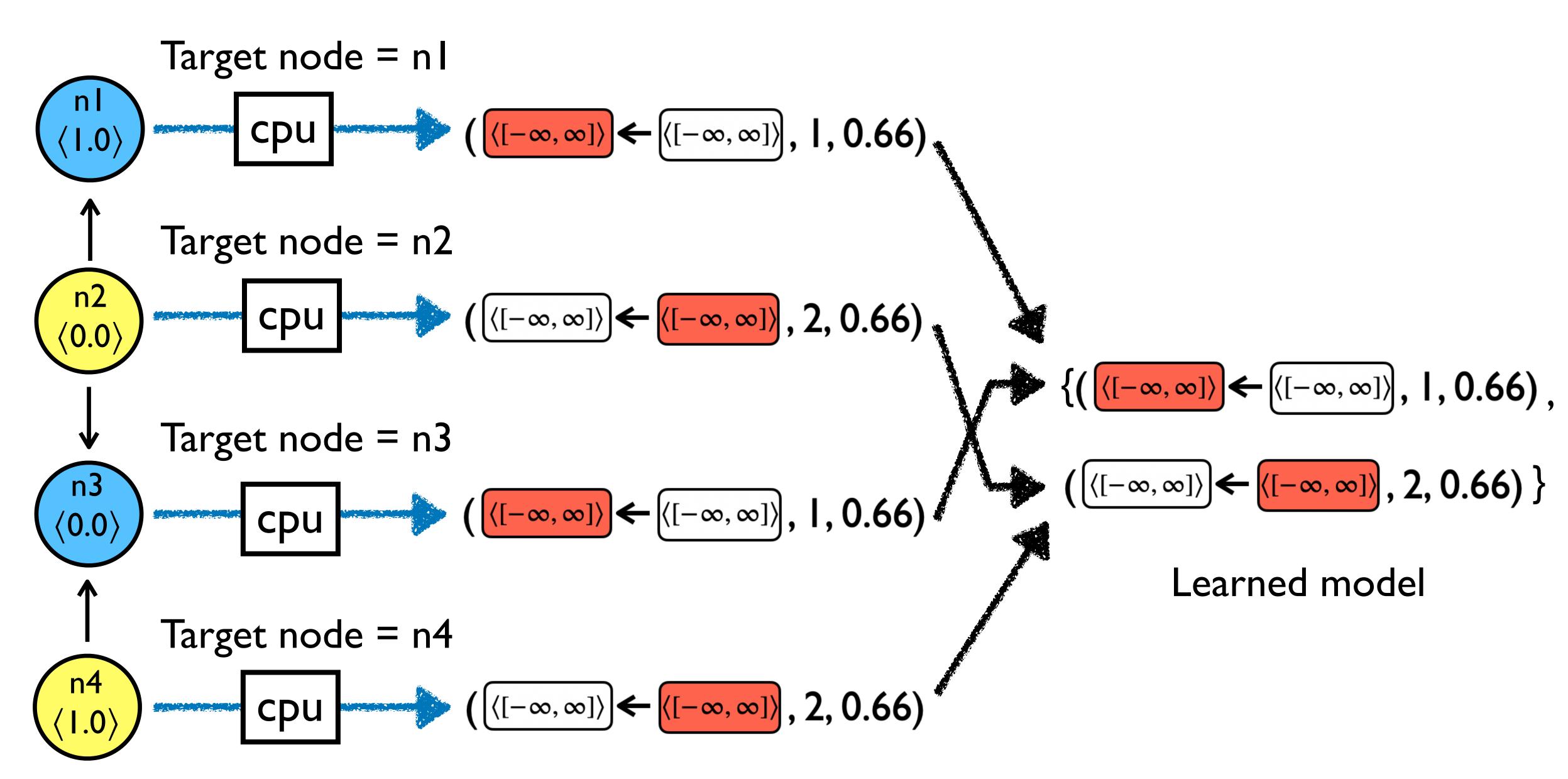
(1) Starts from the most specific program

$$\leftarrow \boxed{\langle [0.0, 0.0] \rangle} \leftarrow \boxed{\langle [0.0, 0.0] \rangle} \leftarrow \boxed{\langle [0.0, 0.0] \rangle} \leftarrow \boxed{\langle [1.0, 1.0] \rangle} \leftarrow \boxed$$

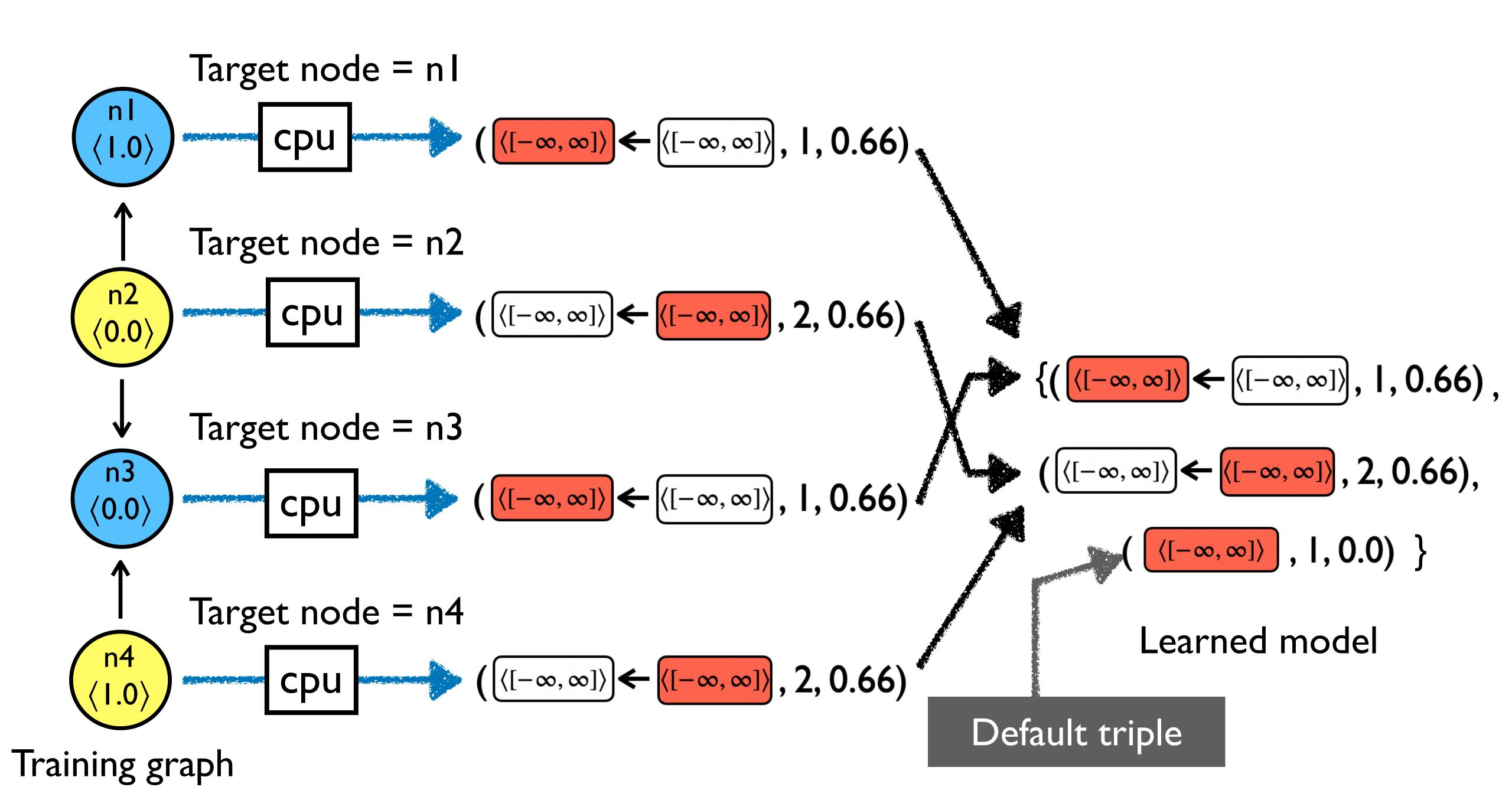
(2) Enumerate possible generalized programs and choose an equal or better scored one

$$\langle [1.0, 1.0] \rangle \leftarrow \langle [0.0, 0.0] \rangle \rightarrow \langle [0.0, 0.0] \rangle$$
 Score: 0.5

- (3) Repeat (2) until all the enumerated programs have lower score
- (4) Return the current program $(([-\infty,\infty]) \leftarrow [([-\infty,\infty])], [abel 1, 0.66)]$



Training graph



Accuracy Comparison

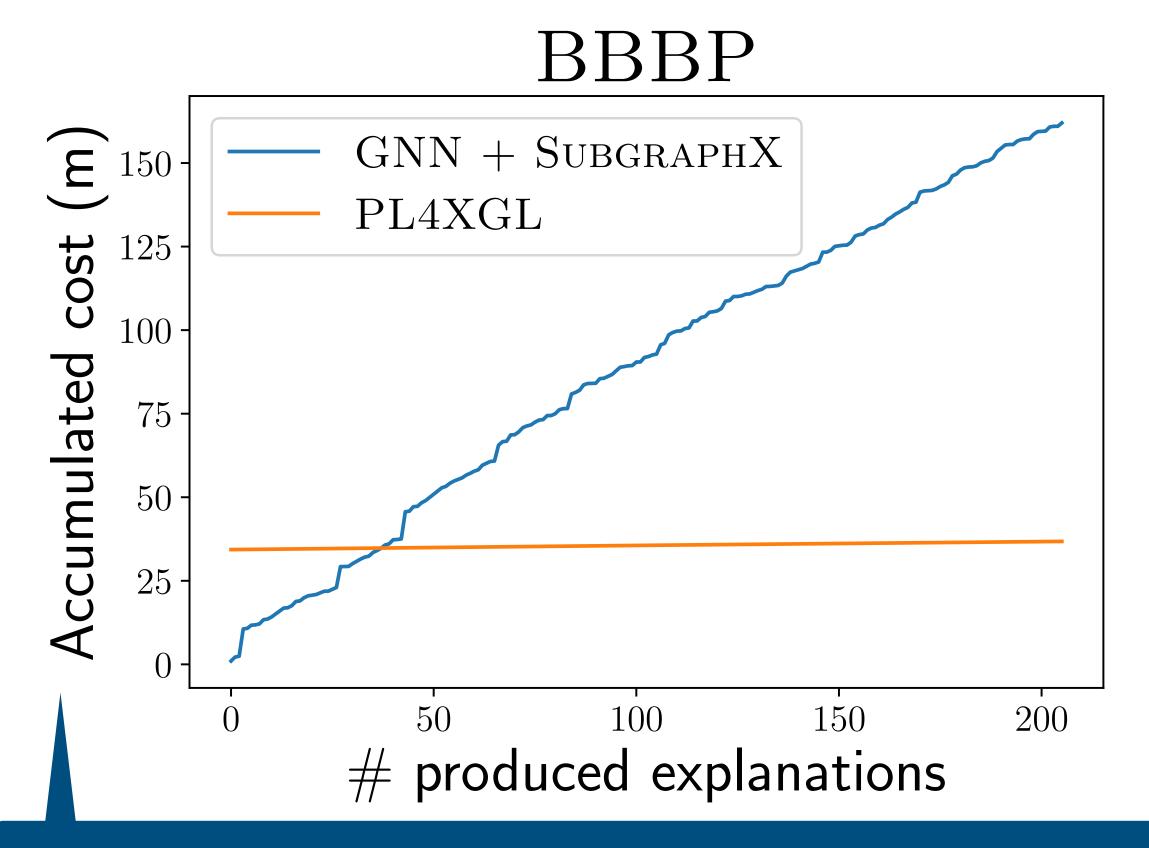
| | GCN | GAT | СневуNет | JKNet | GRAPHSAGE | GIN | DGCN | PL4XGL |
|-------------|----------|----------------|--------------------|----------------|-----------------|----------------|----------------|----------------|
| MUTAG | 80.0±0.0 | 89.0±2.2 | 86.0±4.1 | 68.0±7.5 | 78.0±4.4 | 91.0±5.4 | N/A | 100.0±0.0 |
| BBBP | 83.6±1.4 | 82.3 ± 1.6 | 84.6 ± 1.0 | 85.6 ± 1.9 | 86.6 ± 0.9 | 86.2 ± 1.4 | N/A | 86.8±0.0 |
| BACE | 78.4±2.8 | 52.4 ± 3.3 | 78.9 ± 1.4 | 79.9 ± 1.9 | 79.8 ± 0.8 | 80.9 ± 0.4 | N/A | 80.9±0.0 |
| HIV | 96.4±0.0 | 96.4 ± 0.0 | 96.8 ± 0.2 | 96.8 ± 0.1 | 96.9 ± 0.2 | 96.8 ± 0.1 | N/A | N/A |
| BA-Shapes | 95.1±0.6 | 76.8±2.3 | 97.1±0.0 | 94.3±0.0 | 97.1±0.0 | 92.0±1.1 | 95.1±0.7 | 95.7±0.0 |
| TREE-CYCLES | 97.7±0.0 | 90.9 ± 0.0 | 100.0 ± 0.0 | 98.9 ± 0.0 | 100.0 ± 0.0 | 93.2 ± 0.0 | 99.2 ± 0.5 | 100.0±0.0 |
| Wisconsin | 64.0±0.0 | 49.6±3.1 | 86.4±3.9 | 64.8±1.5 | 92.8±2.9 | 56.0±0.0 | 96.0±0.0 | 88.0±0.0 |
| Texas | 67.7±5.3 | $50.0{\pm}0.0$ | 87.7 ± 2.1 | 68.8 ± 4.3 | 86.6 ± 2.6 | 50.0 ± 0.0 | 86.6 ± 2.6 | 83.3±0.0 |
| Cornell | 58.9±2.6 | $61.1{\pm}0.0$ | 81.0 ± 6.5 | $61.1{\pm}0.0$ | 87.7 ± 2.1 | 61.1 ± 0.0 | 86.6 ± 2.6 | 88.8±0.0 |
| Cora | 85.6±0.3 | 86.4±1.8 | 86.5±5.2 | 84.9±3.5 | 86.3±3.2 | 86.7±0.0 | 83.2±5.9 | 80.0 ± 0.0 |
| CITESEER | 75.2±0.0 | 74.3 ± 0.7 | 79.1±0.9 | 73.7 ± 4.2 | 75.9 ± 2.3 | 75.2 ± 0.0 | 71.3 ± 6.0 | 63.8± 0.0 |
| Pubmed | 82.8±1.1 | 84.7 ± 1.2 | $88.7 \!\pm\! 1.0$ | 83.2 ± 0.4 | 88.0 ± 0.4 | 86.1 ± 0.6 | 85.1 ± 0.6 | 81.4±0.0 |

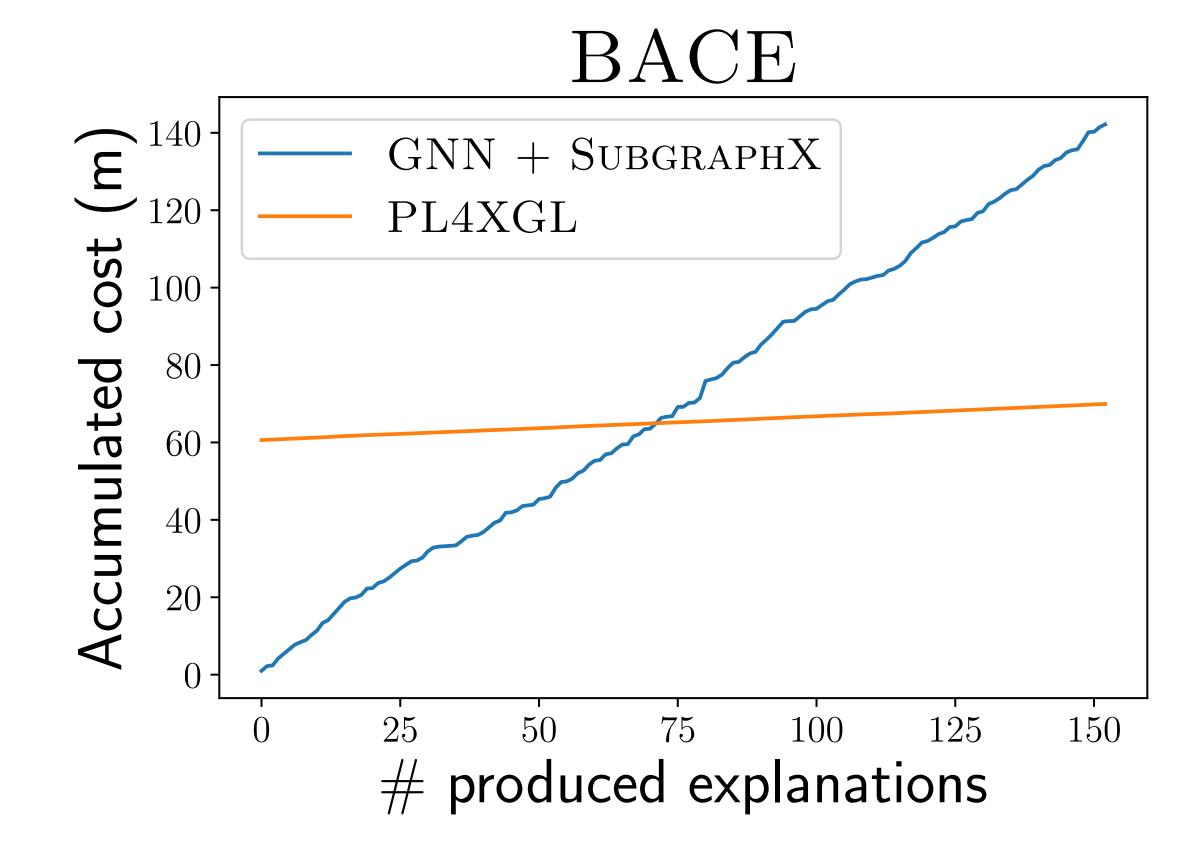
Molecule datasets (graph classification)

| | GCN | GAT | СневуNет | JKNet | GRAPHSAGE | GIN | DGCN | PL4XGL |
|-------------|----------|----------------|-----------------|----------------|----------------|--|----------------|----------------|
| MUTAG | 80.0±0.0 | 89.0±2.2 | 86.0±4.1 | 68.0±7.5 | 78.0 ± 4.4 | 91.0±5.4 | N/A | 100.0±0.0 |
| BBBP | 83.6±1.4 | 82.3 ± 1.6 | 84.6 ± 1.0 | 85.6 ± 1.9 | 86.6 ± 0.9 | 86.2 ± 1.4 | N/A | 86.8±0.0 |
| BACE | 78.4±2.8 | 52.4 ± 3.3 | 78.9 ± 1.4 | 79.9 ± 1.9 | 79.8 ± 0.8 | $80.9 \!\pm\! 0.4$ | N/A | 80.9±0.0 |
| HIV | 96.4±0.0 | 96.4 ± 0.0 | 96.8 ± 0.2 | 96.8 ± 0.1 | 96.9 ± 0.2 | 96.8 ± 0.1 | N/A | |
| BA-Shapes | | | | | | | | |
| TREE-CYCLES | 97.7±0.0 | 90.9±0.0 | 100.0 ± 0.0 | 98.9 PL | 4XGL sho | ows the | best ac | curacy |
| Wisconsin | 64.0±0.0 | 49.6±3.1 | 86.4±3.9 | 64.8 | | the state of the s | | |
| Texas | 67.7±5.3 | 50.0 ± 0.0 | 87.7 ± 2.1 | 68.8 ± 4.3 | 86.6 ± 2.6 | 50.0 ± 0.0 | 86.6±2.6 | 83.3±0.0 |
| Cornell | 58.9±2.6 | 61.1 ± 0.0 | 81.0 ± 6.5 | 61.1 ± 0.0 | 87.7 ± 2.1 | 61.1 ± 0.0 | 86.6 ± 2.6 | 88.8±0.0 |
| Cora | 85.6±0.3 | 86.4±1.8 | 86.5±5.2 | 84.9±3.5 | 86.3±3.2 | 86.7±0.0 | 83.2±5.9 | 80.0 ± 0.0 |
| CITESEER | 75.2±0.0 | 74.3 ± 0.7 | 79.1±0.9 | 73.7 ± 4.2 | 75.9 ± 2.3 | 75.2 ± 0.0 | 71.3 ± 6.0 | 63.8± 0.0 |
| Pubmed | 82.8±1.1 | 84.7±1.2 | 88.7 ± 1.0 | 83.2±0.4 | 88.0 ± 0.4 | 86.1 ± 0.6 | 85.1 ± 0.6 | 81.4±0.0 |

Cost Comparison

Our approach is fast if explanation cost is included

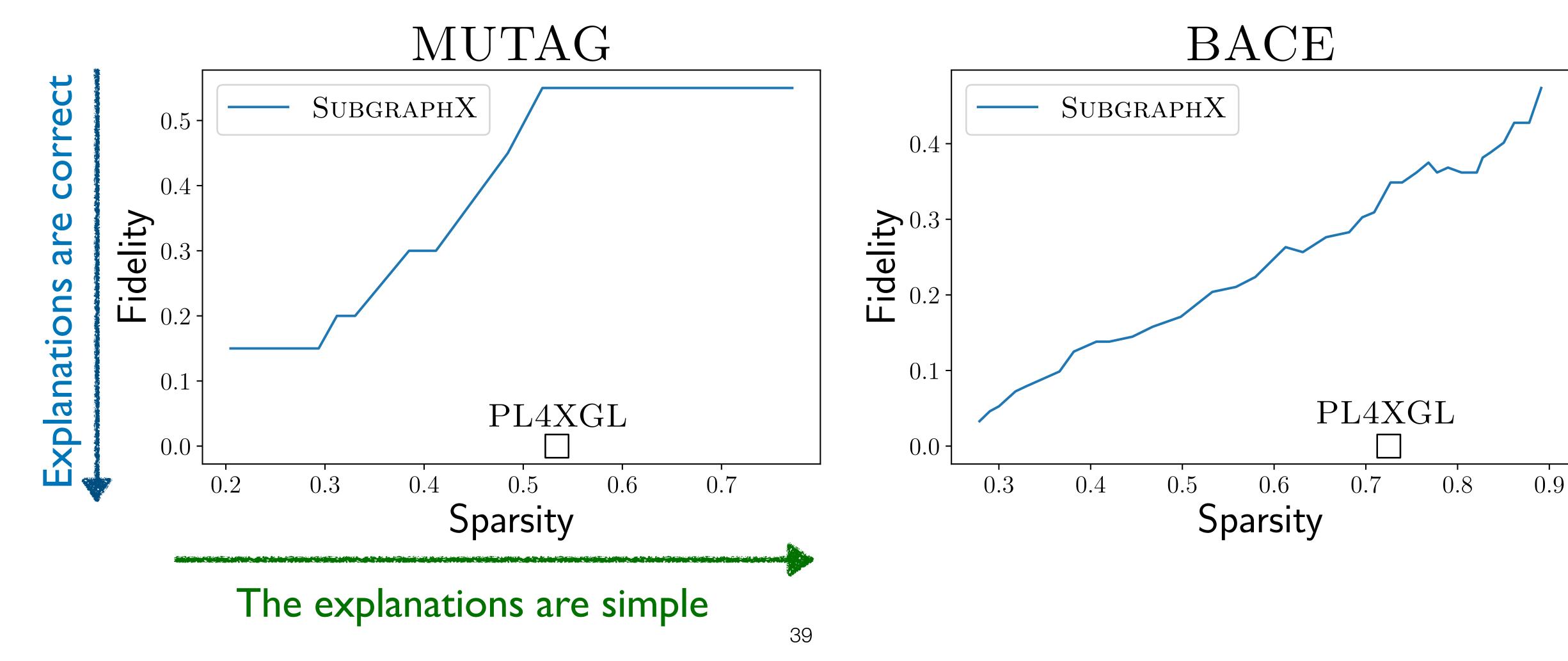




Training + classification + explanation cost

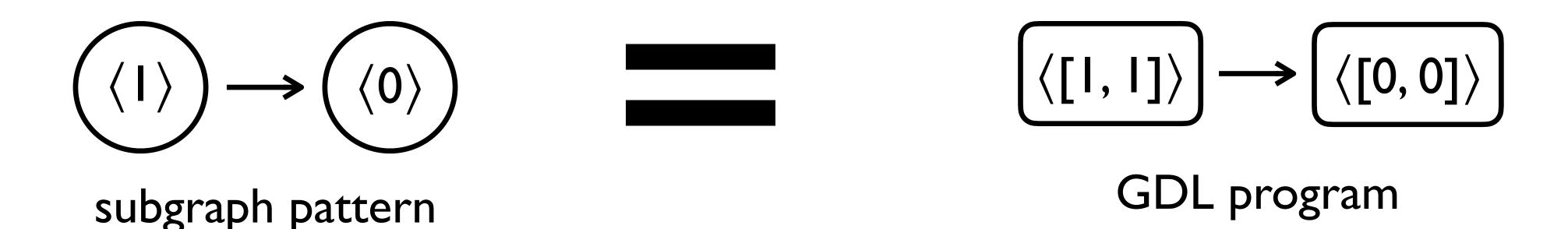
Explainability Comparison

• Our approach provides correct & simple explanations

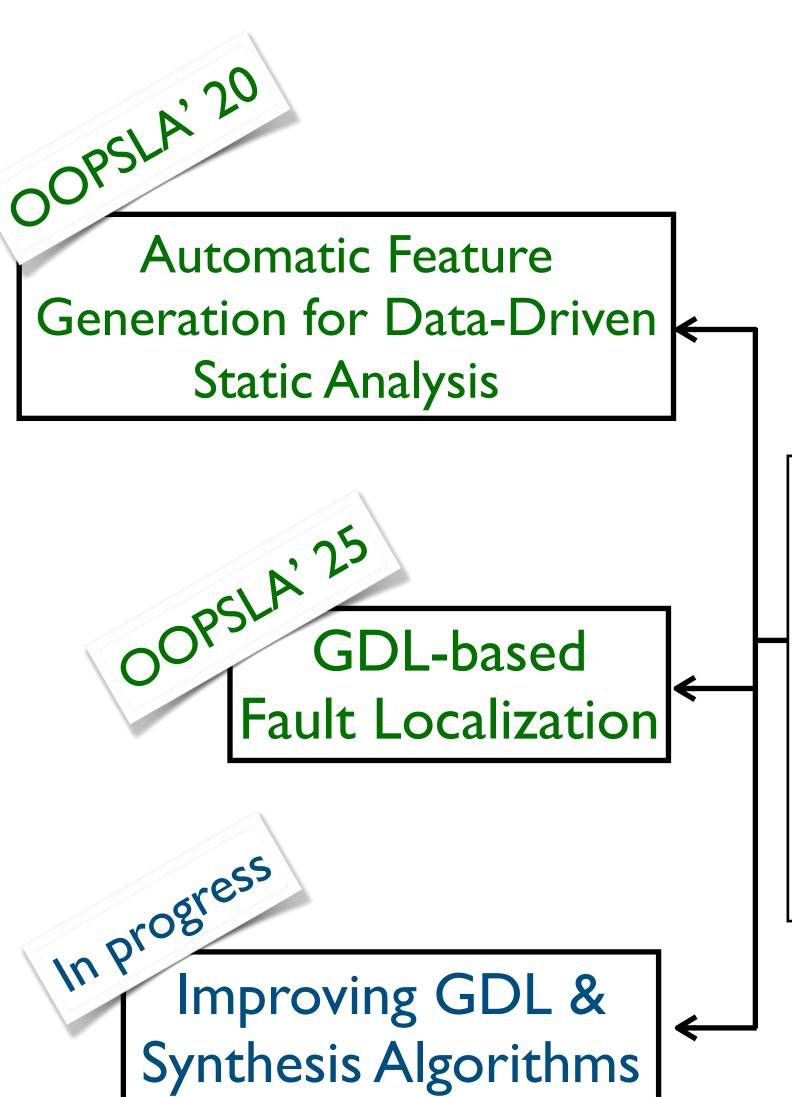


GDL Program vs Subgraph

• GDL is a strictly more expressive than subgraph in graph pattern description



$$\{(0,1]\} \longrightarrow ((0,1]) \qquad \qquad \{(0,0)\} \longrightarrow (0,0), \dots, (1,0)\}$$
GDL program subgraph patterns



Graph Description Language $S = \frac{P}{\delta} \cdot \frac{1}{\delta} \cdot \frac{1}{\delta} \cdot \frac{1}{\delta}$

Programs $P ::= \delta \text{ target } t$ Descriptions $\delta ::= \delta_V \mid \delta_E$

Node Descriptions $\delta_V := \text{node } x < \overline{\phi} > ?$

Edge Descriptions $\delta_E ::= \text{edge } (x, x) < \overline{\phi} > ?$

Target Symbols $t ::= node x \mid edge(x,x) \mid graph$

Intervals $\phi := [n^?, n^?]$

Real Numbers $n := 0.2 \mid 0.7 \mid 6 \mid -8 \dots$

Variables $x := x | y | z | \dots$

Explainable Graph Machine Learning In Progress Improving GNN Using GDL TOPO **GDL**-based Graph Data-mining

GDL-based
GNN Explanation